

FOUNDATION FOR INTELLIGENT PHYSICAL AGENTS

FIPA KIF Content Language Specification

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34 specifications and their current status may be found in the FIPA List of Specifications. A list of terms and abbreviations
35 used in the FIPA specifications may be found in the FIPA Glossary.

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38 specifications and upcoming meetings may be found at <http://www.fipa.org/>.

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1 Scope

This document gives the specification the draft proposed American National Standard (ANSKif) for Knowledge Interchange Format (KIF) as a content language for FIPA ACL (see [FIPA00061]). This specification covers:

- Expression of objects as terms.
- Expression of propositions as sentences.

FIPA KIF currently has no specific way to expresses actions.

85 2 FIPA KIF Specification

86 The aim of this section is to specify KIF as a language for use in the interchange of knowledge among disparate
87 computer systems (created by different programmers, at different times, in different languages, and so forth), especially
88 among FIPA agents.

89
90 FIPA KIF is *not* intended as a primary language for interaction with human users (though it can be used for this
91 purpose). Different computer systems can interact with their users in whatever forms are most appropriate to their
92 applications (for example, Prolog, conceptual graphs, natural language and so forth).

93
94 FIPA KIF is also *not* intended as an internal representation for knowledge *within* computer systems or within closely
95 related sets of computer systems (though the language can be used for this purpose as well). Typically, when a
96 computer system reads a knowledge base in FIPA KIF, it converts the data into its own internal form (specialized
97 pointer structures, arrays, etc.) and all computation is done using these internal forms. When the computer system
98 needs to communicate with another computer system, it maps its internal data structures into FIPA KIF before message
99 transfer.

100
101 The following categorical features are essential to the design of FIPA KIF:

- 102 • The language has declarative semantics. It is possible to understand the meaning of expressions in the language
103 without appeal to an interpreter for manipulating those expressions. In this way, FIPA KIF differs from other
104 languages that are based on specific interpreters, such as Emycin and Prolog.
- 105 • The language is logically comprehensive. At its most general, it provides for the expression of arbitrary logical
106 sentences. In this way, it differs from relational database languages (like SQL) and logic programming languages
107 (like Prolog).
- 108 • The language provides for the representation of knowledge about knowledge. This allows the user to make
109 knowledge representation decisions explicit and permits the user to introduce new knowledge representation
110 constructs without changing the language.

111
112 In addition to these essential features, FIPA KIF is designed to maximize the following additional features (to the extent
113 possible while preserving the preceding features):

- 114 • **Implementability.** Although FIPA KIF is not intended for use within programs as a representation or
115 communication language, it should be usable for that purpose if so desired.
- 116 • **Readability.** Although FIPA KIF is not intended primarily as a language for interaction with humans, human
117 readability facilitates its use in describing representation language semantics, its use as a publication language for
118 example knowledge bases, its use in assisting humans with knowledge base translation problems, etc.

119
120 Unless otherwise stated, all terms and definitions are taken from [ISO10646] and [ISO14481].

121

122 2.1 Syntax

123 2.1.1 Introduction

124 As with many computer-oriented languages, the syntax of FIPA KIF is most easily described in three layers. First, there
125 are the basic characters of the language. These characters can be combined to form lexemes. Finally, the lexemes of
126 the language can be combined to form grammatically legal expressions. Although this layering is not strictly essential to
127 the specification of FIPA KIF, it simplifies the description of the syntax by dealing with white space at the lexeme level
128 and eliminating that detail from the expression level.

129
130 In this section, the syntax of FIPA KIF is presented using a modified BNF notation. All nonterminals and BNF
131 punctuation are written in boldface, while characters in FIPA KIF are expressed in plain font. The notation {x1, ..., xn}

137 means the set of terminals x_1, \dots, x_n . The notation **[nonterminal]** means zero or one instances of **nonterminal**;
 138 **nonterminal*** means zero or more occurrences; **nonterminal+** means one or more occurrences; **nonterminal ^ n**
 139 means **n** occurrences. The notation **nonterminal1 - nonterminal2** refers to all of the members of **nonterminal1** except
 140 for those in **nonterminal2**. The notation **int (n)** denotes the decimal representation of integer **n**. The nonterminals
 141 **space**, **tab**, **return**, **linefeed** and **page** refer to the characters corresponding to ASCII codes 32, 9, 13, 10, and 12,
 142 respectively. The nonterminal **character** denotes the set of all 128 ASCII characters. The nonterminal **empty** denotes
 143 the empty string.
 144

145 2.1.2 Characters

146 The alphabet of FIPA KIF consists of 7 bit blocks of data. In this document, we refer to FIPA KIF data blocks via their
 147 usual ASCII encodings as characters as given in [ISO646].
 148

149 FIPA KIF characters are classified as upper case letters, lower case letters, digits, alpha characters (non-alphabetic
 150 characters that are used in the same way that letters are used), special characters, white space, and other characters
 151 (every ASCII character that is not in one of the other categories):
 152

```

153 upper ::= A | B | C | D | E | F | G | H | I | J | K | L | M |
154         N | O | P | Q | R | S | T | U | V | W | X | Y | Z
155
156 lower ::= a | b | c | d | e | f | g | h | i | j | k | l | m |
157         n | o | p | q | r | s | t | u | v | w | x | y | z
158
159 digit ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
160
161 alpha ::= ! | $ | % | & | * | + | - | . | / | < | = | > | ? |
162         @ | _ | ~ |
163
164 special ::= " | # | ' | ( | ) | , | \ | ^ | '
165
166 white ::= space | tab | return | linefeed | page
167
```

168 A normal character is either an upper case character, a lower case character, a digit, or an alpha character.
 169

```

170 normal ::= upper | lower | digit | alpha
171
```

172 2.1.3 Lexemes

173 The process of converting characters into lexemes is called lexical analysis. The input to this process is a stream of
 174 characters, and the output is a stream of lexemes.
 175

176 The function of a lexical analyser is cyclic. It reads characters from the input string until it encounters a character that
 177 cannot be combined with previous characters to form a legal lexeme. When this happens, it outputs the lexeme
 178 corresponding to the previously read characters. It then starts the process over again with the new character. White
 179 space causes a break in the lexical analysis process but otherwise is discarded.
 180

181 There are five types of lexemes in FIPA KIF: special lexemes, words, character references, character strings and
 182 character blocks. Each special character forms its own lexeme. It cannot be combined with other characters to form
 183 more complex lexemes, except through the escape' syntax described below.
 184

185 A **word** is a contiguous sequence of normal characters or other characters preceded by the escape character \.

```

186 word ::= normal | word normal | word\character
187
```

188 It is possible to include the character \ in a word by preceding it by another occurrence of \, that is, two contiguous
 189 occurrences of \ are interpreted as a single occurrence. For example, the string A\\\'B corresponds to a word
 190 consisting of the four characters A, \, ', and B.
 191
 192

193 Except for characters following \, the lexical analysis of words is case insensitive. The output lexeme for any word
 194 corresponds to the lexeme obtained by converting all letters not following \ to their upper case equivalents. For
 195 example, the word `abc` and the word `ABC` map into the same lexeme. The word `a\bc` maps into the same lexeme as
 196 the word `A\bc`, which is not the same as the lexeme for the word `ABC`, since the second character is lower case.

197

198 A **character reference** consists of the characters #, \, and any character. Character references allow us to refer to
 199 characters as characters and differentiate them from one-character symbols, which may refer to other objects.

200

```
201 charref ::= #\character
```

202

203 A **character string** is a series of characters enclosed in quotation marks. The escape character \ is used to permit the
 204 inclusion of quotation marks and the \ character itself within such strings.

205

```
206 string ::= "quotable"
```

207

```
208 quotable ::= empty | quotable strchar | quotable\character
```

209

```
210 strchar ::= character - {"",\}
```

211

212 Sometimes it is desirable to group together a sequence of arbitrary bits or characters without imposing escape
 213 characters, for example, to encode images, audio, or video in special formats. Character blocks permit this sort of
 214 grouping through the use of a prefix that specifies how many of the following characters are to grouped together in this
 215 way. A **character block** consists of the character # followed by the decimal encoding of a positive integer n , the
 216 character q or Q and then n arbitrary characters.

217

```
218 block ::= # int(n) q character^n | # int(n) Q character^n
```

219

220 For the purpose of grammatical analysis, it is useful to subdivide the class of words a little further, viz. as variables,
 221 operators and constants.

222

223 A **variable** is a word in which the first character is ? or @. A variable that begins with ? is called an **individual variable**.
 224 A variable that begins with an @ is called a **sequence variable**.

225

```
226 variable ::= indvar | seqvar
```

227

```
228 indvar ::= ?word
```

229

```
230 seqvar ::= @word
```

231

232 **Operators** are used in forming complex expressions of various sorts. There are three types of operators in FIPA KIF:

233

- 234 • **Term operators** are used in forming complex terms.

235

- 236 • **Sentence operators** and user operators are used in forming complex sentences.

237

- 238 • **Definition operators** are used in forming definitions.

239

```
240 operator ::= termop | sentop | defop
```

241

```
242 termop ::= value | listof | quote | if
```

243

```
244 sentop ::= holds | = | /= | not | and | or | => | <= | <=> |  
245 forall | exists
```

246

```
247 defop ::= defobject | defunction | defrelation | deflogical |  
248 := | :-> | :<= | :=>
```

249

250 All other words are called **constants**:

251 constant ::= word - variable - operator
 252

253 Semantically, there are four categories of constants in FIPA KIF:
 254

- 255 • **Object constants** are used to denote individual objects.
- 256
- 257 • **Function constants** denote functions on those objects.
- 258
- 259 • **Relation constants** denote relations.
- 260
- 261 • **Logical constants** express conditions about the world and are either true or false.
- 262

263 FIPA KIF is unusual among logical languages in that there is no syntactic distinction among these four types of
 264 constants; any constant can be used where any other constant can be used. The differences between these categories
 265 of constants is entirely semantic.
 266
 267

268 2.1.4 Expressions

269 The legal expressions of FIPA KIF are formed from lexemes according to the rules presented in this section. There are
 270 three disjoint types of expressions in the language:
 271

- 272 • **Terms** are used to denote objects in the world being described.
- 273
- 274 • **Sentences** are used to express facts about the world.
- 275
- 276 • **Definitions** are used to define constants.
- 277

278 There are nine types of terms in FIPA KIF: individual variables, constants, character references, character strings,
 279 character blocks, functional terms, list terms, quotations, and logical terms. Individual variables, constants, character
 280 references, strings and blocks were discussed earlier.
 281

282 term ::= indvar | constant | charref | string | block |
 283 funterm | listterm | quoterm | logterm
 284

285 A **implicit functional term** consists of a constant and an arbitrary number of argument terms, terminated by an
 286 optional sequence variable and surrounded by matching parentheses. Note that there is no syntactic restriction on the
 287 number of argument terms; arity restrictions in FIPA KIF are treated semantically.
 288

289 funterm ::= (constant term* [seqvar])
 290

291 A **explicit functional term** consists of the operator value and one or more argument terms, terminated by an optional
 292 sequence variable and surrounded by matching parentheses.
 293

294 funterm ::= (value term term* [seqvar])
 295

296 A **list term** consists of the `listof` operator and a finite list of terms, terminated by an optional sequence variable and
 297 enclosed in matching parentheses.
 298

299 listterm ::= (listof term* [seqvar])
 300

301 **Quotations** involve the quote operator and an arbitrary *list expression*. A list expression is either an *atom* or a
 302 sequence of list expressions surrounded by parentheses. An atom is either a word or a character reference or a
 303 character string or a character block. Note that the list expression embedded within a quotation need *not* be a legal
 304 expression in FIPA KIF.
 305

306 quoterm ::= (quote listexpr) | 'listexpr


```

307
308     listexpr    ::=  atom | (listexpr*)
309
310     atom       ::=  word | charref | string | block
311

```

312 **Logical terms** involve the `if` and `cond` operators. The `if` form allows for the testing of a single condition or multiple conditions and an optional term at the end allows for the specification of a default value when all of the conditions are false. The `cond` form is similar but groups the pairs of sentences and terms within parentheses and has no optional term at the end.

```

316
317     logterm     ::=  (if logpair+ [term])
318
319     logpair    ::=  sentence term
320
321     logterm     ::=  (cond logitem*)
322
323     logitem    ::=  (sentence term)
324

```

325 The following BNF defines the set of legal sentences in FIPA KIF. There are six types of sentences (logical constants have already been introduced):

```

327
328     sentence   ::=  constant | equation | inequality |
329                   relsent | logsent | quantsent
330

```

331 An **equation** consists of the `=` operator and two terms. An **inequality** consist of the `/=` operator and two terms.

```

332
333     equation   ::=  (= term term)
334
335     inequality ::=  (/= term term)
336

```

337 An **implicit relational sentence** consists of a constant and an arbitrary number of argument terms, terminated by an optional sequence variable. As with functional terms, there is no syntactic restriction on the number of argument terms in a relation sentence.

```

340
341     relsent    ::=  (constant term* [seqvar])
342

```

343 A **explicit relational sentence** consists of the operator `holds` and one or more argument terms, terminated by an optional sequence variable and surrounded by matching parentheses.

```

345
346     relsent    ::=  (holds term term* [seqvar])
347

```

348 It is noteworthy that the syntax of implicit relational sentences is the same as that of implicit functional terms. On the other hand, their meanings are different. Fortunately, the context of each such expression determines its type (as an embedded term in one case or as a top-level sentence or argument to some sentential operator in the other case); and so this slight ambiguity causes no problems.

352 The syntax of **logical sentences** depends on the logical operator involved. A sentence involving the `not` operator is called a negation. A sentence involving the `and` operator is called a conjunction, and the arguments are called conjuncts. A sentence involving the `or` operator is called a disjunction, and the arguments are called disjuncts. A sentence involving the `=>` operator is called an implication, all of its arguments but the last are called antecedents which is called the consequent. A sentence involving the `<=` operator is called a reverse implication, its first argument is called the consequent and the remaining arguments are called the antecedents. A sentence involving the `<=>` operator is called an equivalence.

```

360
361     logsent    ::=  (not sentence) |
362                   (and sentence*) |
363                   (or sentence*) |
364                   (=> sentence* sentence) |
365                   (<= sentence sentence*) |

```

366 (=> sentence sentence)

367

368 There are two types of **quantified sentences**: a universally quantified sentence is signalled by the use of the `forall`
 369 operator, and an existentially quantified sentence is signalled by the use of the `exists` operator. The first argument in
 370 each case is a list of variable specifications. A variable specification is either a variable or a list consisting of a variable
 371 and a term denoting a relation that restricts the domain of the specified variable.

372

373 `quantsent ::= (forall (varspec+) sentence) |`
 374 `(exists (varspec+) sentence)`

375

376 `varspec ::= variable | (variable constant)`

377

378 Note that, according to these rules, it is permissible to write sentences with free variables, that is, variables that do not
 379 occur within the scope of any enclosing quantifiers. The significance of the free variables in a sentence depends on the
 380 use of the sentence. When we assert the truth of a sentence with free variables, we are, in effect, saying that the
 381 sentence is true for all values of the free variables, that is, the variables are universally quantified. When we ask
 382 whether a sentence with free variables is true, we are, in effect, asking whether there are any values for the free
 383 variables for which the sentence is true, i.e. the variables are existentially quantified.

384

385 The following BNF defines the set of legal FIPA KIF definitions. There are three types of definitions: unrestricted,
 386 complete and partial. Within each type, there are four cases, one for each category of constant. Object constants are
 387 defined using the `defobject` operator, function constants are defined using the `deffunction` operator, relation
 388 constants are defined using the `defrelation` operator and logical constants are defined using the `deflogical`
 389 operator.

390

391 `definition ::= unrestricted | complete | partial`

392

393 `unrestricted ::= (defobject constant [string] sentence*)`
 394 `| (deffunction constant [string] sentence*)`
 395 `| (defrelation constant [string] sentence*)`
 396 `| (deflogical constant [string] sentence*)`

397

398 `complete ::= (defobject constant [string] := term)`
 399 `| (deffunction constant (indvar* [seqvar]) [string] := term)`
 400 `| (defrelation constant (indvar* [seqvar]) [string] := sentence)`
 401 `| (deflogical constant [string] := sentence)`

402

403 `partial ::= (defobject constant [string] :-> indvar <= sentence)`
 404 `| (defobject constant [string] :-> indvar :=> sentence)`
 405 `| (deffunction constant (indvar* [seqvar])`
 406 `[string] :-> indvar <= sentence)`
 407 `| (deffunction constant (indvar* [seqvar])`
 408 `[string] :-> indvar :=> sentence)`
 409 `| (defrelation constant (indvar* [seqvar])`
 410 `[string] <= sentence)`
 411 `| (defrelation constant (indvar* [seqvar])`
 412 `[string] :=> sentence)`
 413 `| (deflogical constant [string] <= sentence)`
 414 `| (deflogical constant [string] :=> sentence)`

415

416 A **form** in FIPA KIF is either a sentence or a definition.

417

418 `form ::= sentence | definition`

419

420 It is important to note that definitions are top level constructs. While definitions contain sentences, they are not
 421 themselves sentences and, therefore, cannot be written as constituent parts of sentences or other definitions (unless
 422 they occur inside of a quotation.

423

424 A **knowledge base** is a finite set of forms. It is important to keep in mind that a knowledge base is a *set* of sentences,
 425 not a *sequence*; and, therefore, the order of forms within a knowledge base is unimportant. Order *may* have heuristic

426 value to deductive programs by suggesting an order in which to use those sentences; however, this implicit approach to
 427 knowledge exchange lies outside of the definition of FIPA KIF.
 428

429 2.2 Basics

430 2.2.1 Introduction

431 The basis for the semantics of FIPA KIF is a conceptualization of the world in terms of objects and relations among
 432 those objects.
 433

434 A *universe of discourse* is the set of all objects presumed or hypothesized to exist in the world. The notion of object
 435 used here is quite broad. Objects can be concrete, for example, a specific carbon atom, Confucius, the Sun or abstract,
 436 such as the number 2, the set of all integers or the concept of justice. Objects can be primitive or composite, for
 437 example, a circuit that consists of many sub circuits. Objects can even be fictional, for example, a unicorn, Sherlock
 438 Holmes, etc.
 439

440 Different users of a declarative representation language, like FIPA KIF, are likely to have different universes of
 441 discourse. FIPA KIF is conceptually promiscuous in that it does not require every user to share the same universe of
 442 discourse. On the other hand, FIPA KIF is conceptually grounded in that every universe of discourse is required to
 443 include certain basic objects.
 444

445 The following basic objects must occur in every universe of discourse:

- 446 • All numbers, real and complex.
- 447 • All ASCII characters.
- 448 • All finite strings of ASCII characters.
- 449 • Words and the things they represent.
- 450 • All finite lists of objects in the universe of discourse.
- 451 • Bottom. A distinguished object that occurs as the value of a partial when that function is applied to arguments for
 452 which the function make no sense.
 453
- 454 • All finite lists of objects in the universe of discourse.
- 455 • Bottom. A distinguished object that occurs as the value of a partial when that function is applied to arguments for
 456 which the function make no sense.
 457
- 458 • Bottom. A distinguished object that occurs as the value of a partial when that function is applied to arguments for
 459 which the function make no sense.

460 Remember, that to these basic elements, the user can add whatever non-basic objects seem useful.
 461

462 In FIPA KIF, relationships among objects take the form of relations. Formally, a relation is defined as an arbitrary set of
 463 finite lists of objects (of possibly varying lengths). Each list is a selection of objects that jointly satisfy the relation. For
 464 example, the < relation on numbers contains the list <2, 3>, indicating that 2 is less than 3.
 465

466 A function is a special kind of relation. For every finite sequence of objects (called the arguments), a function associates
 467 a unique object (called the value). More formally, a function is defined as a set of finite lists of objects, one for each
 468 combination of possible arguments. In each list, the initial elements are the arguments, and the final element is the
 469 value. For example, the $1+$ function contains the list <2, 3>, indicating that integer successor of 2 is 3.
 470

471 Note that both functions and relations are defined as sets of lists. In fact, every function is a relation. However, not
 472 every relation is a function. In a function, there cannot be two lists that disagree on only the last element, since this
 473 would be tantamount to the function having two values for one combination of arguments. By contrast, in a relation,
 474 there can be any number of lists that agree on all but the last element. For example, the list <2, 3> is a member of the
 475 $1+$ function, and there is no other list of length 2 with 2 as its first argument, that is, there is only one successor for 2. By
 476 contrast, the < relation contains the lists <2, 3>, <2, 4>, <2, 5>, and so forth, indicating that 2 is less than 3, 4, 5, and so
 477 forth.
 478

479 Many mathematicians require that functions and relations have fixed arity, that is, they require that all of the lists
 480 comprising a relation have the same length. The definitions here allow for relations with variable arity; it is perfectly
 481 acceptable for a function or a relation to contain lists of different lengths. For example, the relation `<` contains the lists
 482 `<2, 3>` and `<2, 3, 4>`, reflecting the fact that 2 is less than 3 and the fact that 2 is less than 3 and 3 is less than 4. This
 483 flexibility is not essential, but it is extremely convenient and poses no significant theoretical problems.
 484

485 **2.2.2 Bottom**

486 In FIPA KIF, all functions are total, that is, there is a value for every combination of arguments. In order to allow a user
 487 to express the idea that a function is not meaningful for certain arguments, FIPA KIF assumes that there is a special
 488 “undefined” object in the universe and provides the object constant `bottom` to refer to this object.
 489

490 **2.2.3 Functional Terms**

491 The value of a functional term without a terminating sequence variable is obtained by applying the function denoted by
 492 the function constant in the term to the objects denoted by the arguments.
 493

494 For example, the value of the term `(+ 2 3)` is obtained by applying the addition function (the function denoted by `+`) to
 495 the numbers 2 and 3 (the objects denoted by the object constants `2` and `3`) to obtain the value 5, which is the value of
 496 the object constant `5`.
 497

498 If a functional term has a terminating sequence variable, the value is obtained by applying the function to the sequence
 499 of arguments formed from the values of the terms that precede the sequence variable and the values in the sequence
 500 denoted by the sequence variable.
 501

502 Assume, for example, that the sequence variable `@1` has as value the sequence 2, 3, 4. Then, the value of the term `(+
 503 1 @1)` is obtained by applying the addition function to the numbers 1, 2, 3, and 4 to obtain the value 10, which is the
 504 value of the object constant `10`.
 505

506 **2.2.4 Relational Sentences**

507 A simple relational sentence without a terminating sequence variable is true if and only if the relation denoted by the
 508 relation constant in the sentence is true of the objects denoted by the arguments. Equivalently, viewing a relation as a
 509 set of tuples, we say that the relational sentence is true if and only if the tuple of objects formed from the values of the
 510 arguments is a member of the set of tuples denoted by the relation constant.
 511

512 If a relational sentence terminates in a sequence variable, the sentence is true if and only if the relation contains the
 513 tuple consisting of the values of the terms that precede the sequence variable together with the objects in the sequence
 514 denoted by the variable.
 515

516 **2.2.5 Equations and Inequalities**

517 An equation is true if and only if the terms in the equation refer to the same object in the universe of discourse. An
 518 inequality is true if and only if the terms in the equation refer to distinct objects in the universe of discourse.
 519

520 **2.2.6 True and False**

521 The truth-value of true is `true`, and the truth-value of false is `false`.
 522

523 **2.3 Logic**524 **2.3.1 Logical Terms**

525 The value of a logical term involving the `if` operator is the value of the term following the first true sentence in the
 526 argument list. For example, the term `(if (> 1 2) 1 (> 2 1) 2 0)` is equivalent to 2.

527
 528 If none of the embedded sentences of a logical term involving the `if` operator is true and there is an isolated term at the
 529 end, the value of the conditional term is the value of that isolated term. For example, if the object constant `a` denotes a
 530 number, then the term `(if (> a 0) a (- a))` denotes the absolute value of that number.

531
 532 If none of the embedded sentences is true and there is no isolated term at the end, the value is undefined (that is,
 533 bottom). In other words, the term `(if (p a) a)` is equivalent to `(if (p a) a bottom)`. The value of a logical term
 534 involving the `cond` operator is the value of the term following the first true sentence in the argument list. For example,
 535 the term `(cond ((> 1 2) 1) ((> 2 1) 2))` is equivalent to 2.

536
 537 If none of the embedded sentences is true, the value is undefined. In other words, the term `(cond ((p a) a))` is
 538 equivalent to `(cond ((p a) a) (true bottom))`.

539

540 **2.3.2 Logical Sentences**

541 A negation is true if and only if the negated sentence is false.

542

543 A conjunction is true if and only if every conjunct is true.

544

545 A disjunction is true if and only if at least one of the disjuncts is true.

546

547 If every antecedent in an implication is true, then the implication as a whole is true if and only if the consequent is true. If
 548 any of the antecedents is false, then the implication as a whole is true, regardless of the truth-value of the consequent.

549

550 A reverse implication is just an implication with the consequent and antecedents reversed.

551

552 An equivalence is equivalent to the conjunction of an implication and a reverse implication.

553

554 **2.3.3 Quantified Sentences**

555 A simple existentially quantified sentence (one in which the first argument is a list of variables) is true if and only if the
 556 embedded sentence is true for some value of the variables mentioned in the first argument.

557

558 A simple universally quantified sentence (one in which the first argument is a list of variables) is true if and only if the
 559 embedded sentence is true for every value of the variables mentioned in the first argument.

560

561 Quantified sentences with complicated variables specifications can be converted into simple quantified sentences by
 562 replacing each complicated variable specification by the variable in the specification and adding an appropriate
 563 condition into the body of the sentence. Note that, in the case of a set restriction, it may be necessary to rename
 564 variables to avoid conflicts. The following pairs of sentences show the transformation from complex quantified
 565 sentences to simple quantified sentences.

566

```
567 (forall (... (?x r) ...) s)
568 (forall (... ?x ...) (=> (r ?x) s))
```

569

```
570 (exists (... (?x r) ...) s)
571 (exists (... ?x ...) (and (r ?x) s))
```

572

573 Note that the significance of free variables in quantifier-free sentences depends on context. Free variables in an
 574 assertion are assumed to be universally quantified. Free variables in a query are assumed to be existentially quantified.

575 In other words, the meaning of free variables is determined by the way in which FIPA KIF is used. It cannot be
 576 unambiguously defined within FIPA KIF itself. To be certain of the usage in all contexts, use explicit quantifiers.
 577

578 2.3.4 Definitions

579 The definitional operators in FIPA KIF allow us to state sentences that are true “by definition” in a way that distinguishes
 580 them from sentences that express contingent properties of the world. Definitions have no truth-values in the usual
 581 sense; they are so because we say that they are so.
 582

583 On the other hand, definitions have content: sentences that allow us to derive other sentences as conclusions. In FIPA
 584 KIF, every definition has a corresponding set of sentences, called the content of the definition.
 585

586 The `defobject` operator is used to define objects. The legal forms are shown below, together with their content. In the
 587 first case, the content is the equation involving the object constant in the definition with the defining term. In the second
 588 case, the content is the conjunction of the constituent sentences.
 589

```
590 (defobject s := t)
591     (= s t)
```

```
593 (defobject s p1 ... pn)
594     (and p1 ... pn)
```

```
596 (defobject s :-> v :=> p)
597     (=> (= s v) p)
```

```
599 (defobject s :-> v :<= p)
600     (<= (= s v) p)
```

601
 602 The `deffunction` operator is used to define functions. Again, the legal forms are shown below, together with their
 603 defining axioms. In the first case, the content is the equation involving the term formed from the function constant in the
 604 definition and the variables in its argument list and the defining term. In the second case, as with object definitions, the
 605 content is the conjunction of the constituent sentences.
 606

```
607 (deffunction f (v1 ...vn) := t)
608     (= (f v1 ...vn) t)
```

```
610 (deffunction f p1 ...pn)
611     (and p1 ...pn)
```

```
613 (deffunction f (v1 ... vn) :-> v :=> p)
614     (=> (= (f v1 ... vn) v) p)
```

```
616 (deffunction f (v1 ... vn) :-> v :<= p)
617     (<= (= (f v1 ... vn) v) p)
```

618
 619 The `defrelation` operator is used to define relations. The legal forms are shown below, together with their defining
 620 axioms. In the first case, the content is the equivalence relating the relational sentence formed from the relation
 621 constant in the definition and the variables in its argument list and the defining sentence. In the second case, as with
 622 object and function definitions, the content is the conjunction of the constituent sentences.
 623

```
624 (defrelation r (v1 ...vn) := p)
625     (<=> (r v1 ...vn) p)
```

```
627 (defrelation r p1 ...pn)
628     (and p1 ...pn)
```

```
630 (defrelation r (v1 ... vn) :=> p)
631     (=> (r v1 ... vn) p))
```

```
633 (defrelation r (v1 ... vn) :<= p)
```

634 (\leq (r v1 ... vn) p))
 635

636 2.4 Numbers

637 2.4.1 Introduction

638 The referent of every numerical constant in FIPA KIF is assumed to be the number for which that constant is the base
 639 10 representation. Among other things, this means that we can infer inequality of all distinct numerical constants, i.e. for
 640 every t_1 and distinct t_2 the following sentence is true.

641 (\neq t1 t2)
 642

643 We use the intended meaning of numerical constants in defining the numerical functions and relations in this section. In
 644 particular, we require that these functions and relations behave correctly on all numbers represented in this way.
 645

646 Note that this does mean that it is incorrect to apply these functions and relations to terms other than numbers. For
 647 example, a non-numerical term may refer to a number, for example, the term two may be defined to be the same as the
 648 number 2 in which case it is perfectly proper to write (+ two two).
 649

650 The user may also want to extend these functions and relations to apply to objects other than numbers, for example,
 651 sets and lists.
 652
 653

654 2.4.2 Functions on Numbers

- 655 • *
- 656 If t_1, \dots, t_n denote numbers, then the term (\ast t1 ... tn) denotes the product of those numbers.
 657
- 658 • +
- 659 If t_1, \dots, t_n are numerical constants, then the term (+ t1 ... tn) denotes the sum t of the numbers
 660 corresponding to those constants.
 661
- 662 • -
- 663 If t and t_1, \dots, t_n denote numbers, then the term (- t t1 ... tn) denotes the difference between the number
 664 denoted by t and the numbers denoted by t_1 through t_n . An exception occurs when $n=0$, in which case the term
 665 denotes the negation of the number denoted by t .
 666
- 667 • /
- 668 If t_1, \dots, t_n are numbers, then the term (/ t1 ... tn) denotes the result t obtained by dividing the number
 669 denoted by t_1 by the numbers denoted by t_2 through t_n . An exception occurs when $n=1$, in which case the term
 670 denotes the reciprocal t of the number denoted by t_1 .
 671
- 672 • 1+
- 673 The term (1+ t) denotes the sum of the object denoted by t and 1.
 674
 675 (deffunction 1+ (?x) := (+ ?x 1))
 676
- 677 • 1-
- 678 The term (1- t) denotes the difference of the object denoted by t and 1.
 679
 680 (deffunction 1- (?x) := (- ?x 1))
 681
- 682 • abs
- 683 The term (abs t) denotes the absolute value of the object denoted by t .
 684
 685 (deffunction abs (?x) := (if (\geq ?x 0) ?x (- ?x)))

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- `ceiling`
If t denotes a real number, then the term `(ceiling t)` denotes the smallest integer greater than or equal to the number denoted by t .
- `denominator`
The term `(denominator t)` denotes the denominator of the canonical reduced form of the object denoted by t .
- `expt`
The term `(expt t1 t2)` denotes the object denoted by t_1 raised to the power the object denoted by t_2 .
- `floor`
The term `(floor t)` denotes the largest integer less than the object denoted by t .
- `gcd`
The term `(gcd t1 ... tn)` denotes the greatest common divisor of the objects denoted by t_1 through t_n .
- `imagpart`
The term `(imagpart t)` denotes the imaginary part of the object denoted by t .
- `lcm`
The term `(lcm t1 ... tn)` denotes the least common multiple of the objects denoted by t_1, \dots, t_n .
- `log`
The term `(log t1 t2)` denotes the logarithm of the object denoted by t_1 in the base denoted by t_2 .
- `max`
The term `(max t1 ... tk)` denotes the largest object denoted by t_1 through t_n .
- `min`
The term `(min t1 ... tk)` denotes the smallest object denoted by t_1 through t_n .
- `mod`
The term `(mod t1 t2)` denotes the root of the object denoted by t_1 modulo the object denoted by t_2 . The result will have the same sign as denoted by t_1 .
- `numerator`
The term `(numerator t)` denotes the numerator of the canonical reduced form of the object denoted by t .
- `realpart`
The term `(realpart t)` denotes the real part of the object denoted by t .
- `rem`
The term `(rem t1 t2)` denotes the remainder of the object denoted by t_1 divided by the object denoted by t_2 . The result has the same sign as the object denoted by t_2 .
- `round`
The term `(round t)` denotes the integer nearest to the object denoted by t . If the object denoted by t is halfway between two integers (for example 3.5), it denotes the nearest integer divisible by 2.
- `sqrt`
The term `(sqrt t)` denotes the principal square root of the object denoted by t .
- `truncate`
The term `(truncate t)` denotes the largest integer less than the object denoted by t .

741

742 **2.4.3 Relations on Numbers**

- 743 • integer

744 The sentence `(integer t)` means that the object denoted by `t` is an integer.

745

- 746 • real

747 The sentence `(real t)` means that the object denoted by `t` is a real number.

748

- 749 • complex

750 The sentence `(complex t)` means that the object denoted by `t` is a complex number.

751

752 `(defrelation number (?x) := (or (real ?x) (complex ?x)))`

753

754 `(defrelation natural (?x) := (and (integer ?x) (>= ?x 0)))`

755

756 `(defrelation rational (?x) :=`

757

757 `(exists (?y) (and (integer ?y) (integer (* ?x ?y))))`

758

- 759 • approx

760 The sentence `(approx t1 t2 t)` is true if and only if the number denoted by `t1` is “approximately equal” to the number denoted by `t2`, that is, the absolute value of the difference between the numbers denoted by `t1` and `t2` is less than or equal to the number denoted by `t`.

761

762

763

764

765

766

767

767 `(defrelation > (?x ?y) := (< ?y ?x))`

768

768 `(defrelation =< (?x ?y) := (or (= ?x ?y) (< ?x ?y)))`

769

769 `(defrelation >= (?x ?y) := (or (> ?x ?y) (= ?x ?y)))`

770

770 `(defrelation positive (?x) := (> ?x 0))`

771

771 `(defrelation negative (?x) := (< ?x 0))`

772

772 `(defrelation zero (?x) := (= ?x 0))`

773

773 `(defrelation odd (?x) := (integer (/ (+ ?x 1) 2))`

774

774 `(defrelation even (?x) := (integer (/ ?x 2))`

775

776

777

778

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788

789

789 `(listof mary (listof tom dick harry) sally)`

790

791

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796

783 **2.5 Lists**

784 A list is a finite sequence of objects. Any objects in the universe of discourse may be elements of a list.

785

786 In FIPA KIF, we use the term `(listof t1 ... tk)` to denote the list of objects denoted by `t1`, ..., `tk`. For example, the following expression denotes the list of an object named `mary`, a list of objects named `tom`, `dick` and `harry`, and an object named `sally`.

787

788

789

790

791

792

793

794

795

796

795 `(defrelation list (?x) := (exists (@1) (= ?x (listof @1))))`

796

797 The object constant `nil` denotes the empty list and also tests whether or not an object is the empty list. The relation
 798 constants `single`, `double` and `triple` allow us to assert the length of lists containing one, two or three elements,
 799 respectively.

```
800 (defobject nil := (listof))
801
802 (defrelation null (?l) := (= ?l (listof)))
803
804 (defrelation single (?l) := (exists (?x) (= ?l (listof ?x))))
805
806 (defrelation double (?l) := (exists (?x ?y) (= ?l (listof ?x ?y))))
807
808 (defrelation triple (?l) := (exists (?x ?y ?z) (= ?l (listof ?x ?y ?z))))
809
810
```

811 The functions `first`, `rest`, `last` and `butlast` each take a single list as argument and select individual items or sub
 812 lists from those lists.

```
813 (deffunction first (?l) := (if (= (listof ?x @items) ?l) ?x)
814
815 (deffunction rest (?l) :=
816   (cond ((null ?l) ?l)
817         ((= ?l (listof ?x @items)) (listof @items)))
818
819 (deffunction last (?l) :=
820   (cond ((null ?l) bottom) ((null (rest ?l)) (first ?l))
821         (true (last (rest ?l))))
822
823 (deffunction butlast (?l) :=
824   (cond ((null ?l) bottom) ((null (rest ?l)) nil)
825         (true (cons (first ?l) (butlast (rest ?l)))))
826
827
```

828 The sentence `(item t1 t2)` is true if and only if the object denoted by `t2` is a non-empty list and the object denoted by
 829 `t1` is either the first item of that list or an item in the rest of the list.

```
830 (defrelation item (?x ?l) :=
831   (and (list ?l) (not (null ?l))
832        (or (= ?x (first ?l)) (item ?x (rest ?l))))
833
834
```

835 The sentence `(sublist t1 t2)` is true if and only if the object denoted by `t1` is a final segment of the list denoted by
 836 `t2`.

```
837 (defrelation sublist (?l1 ?l2) :=
838   (and (list ?l1) (list ?l2)
839        (or (= ?l1 ?l2) (sublist ?l1 (rest ?l2))))
840
841
```

842 The function `cons` adds the object specified as its first argument to the front of the list specified as its second argument.

```
843 (deffunction cons (?x ?l) :=
844   (if (= ?l (listof @l)) (listof ?x @l)))
845
846
```

847 The function `append` adds the items in the list specified as its first argument to the list specified as its second
 848 argument. The function `revappend` is similar, except that it adds the items in reverse order.

```
849 (deffunction append (?l1 ?l2) :=
850   (cond ((null ?l1) (if (list ?l2) ?l2))
851         ((list ?l1) (cons (first ?l1) (append (rest ?l1) ?l2))))
852
853 (deffunction revappend (?l1 ?l2) :=
854   (cond ((null ?l1) (if (list ?l2) ?l2))
855         ((list ?l1) (revappend (rest ?l1) (cons (first ?l1) ?l2))))
856
```

857

858 The function `reverse` produces a list in which the order of items is the reverse of that in the list supplied as its single
859 argument.

860

```
861 (deffunction reverse (?l) := (revappend ?l (listof)))
```

862

863 The functions `adjoin` and `remove` construct lists by adding or removing objects from the lists specified as their
864 arguments.

865

```
866 (deffunction adjoin (?x ?l) := (if (item ?x ?l) ?l (cons ?x ?l)))
```

867

```
868 (deffunction remove (?x ?l) :=
869   (cond ((null ?l) nil) ((and (= ?x (first ?l)) (list ?l))
870     (remove ?x (rest ?l)))
871     ((list ?l) (cons ?x (remove ?x (rest ?l))))))
```

872

873 The value of `subst` is the object or list obtained by substituting the object supplied as first argument for all occurrences
874 of the object supplied as second argument in the object or list supplied as third argument.

875

```
876 (deffunction subst (?x ?y ?z) :=
877   (cond ((= ?y ?z) ?x) ((null ?z) nil)
878     ((list ?z) (cons (subst ?x ?y (first ?z))
879       (subst ?x ?y (rest ?z))))
880     (true ?z)))
```

881

882 The function `length` gives the number of items in a list. The function `nth` returns the item in the list specified as its first
883 argument in the position specified as its second argument. The function `nthrest` returns the list specified as its first
884 argument minus the first n items, where n is the number specified as its second argument.

885

```
886 (deffunction length (?l) :=
887   (cond ((null ?l) 0)
888     ((list ?l) (1+ (length (rest ?l)))))
```

889

```
890 (deffunction nth (?l ?n) :=
891   (cond ((= ?n 1) (first ?l))
892     ((and (list ?l) (positive ?n)) (nth (rest ?l) (1- ?n))))
```

893

```
894 (deffunction nthrest (?l ?n) :=
895   (cond ((= ?n 0) (if (list ?l) ?l))
896     ((and (list ?l) (positive ?n)) (nthrest (rest ?l) (1- ?n))))
```

897

898 2.6 Characters and Strings

899 2.6.1 Characters

900 A character is a printed symbol, such as a digit or a letter. There are 128 distinct characters known to FIPA KIF,
901 corresponding to the 128 possible combinations of bits in the ASCII encoding. In FIPA KIF, there are two ways to refer
902 to characters.

903

904 The first method is use of the `charref` syntax, that is, the characters `#` and `\`, followed by the character to be
905 represented. While this method works for all 128 characters, it is less than ideal for documents like this one, because of
906 the difficulty of writing out non-printing characters. Using this method, it is also difficult to assert properties of some
907 classes of characters. For this reason, FIPA KIF supports an alternative method of specification, viz. the use of the 7 bit
908 code corresponding to the character. The relationship between characters and their numerical codes is given via the
909 functions `char-code` and `code-char`. The former maps the n th character cn into the corresponding 7-bit integer n , and
910 the latter maps a 7-bit integer n into the corresponding character cn . The values of these functions on all other
911 arguments are undefined.

912

```

913      (= (char-code #\cn) n)
914
915      (= (code-char n) #\cn)

```

917 The relation `character` is true of the characters of FIPA KIF and no other objects.

```

918
919      (defrelation character (?x) :=
920          (exists ((?n natural-number)) (and (>= ?n 0) (< ?n 128)
921              (= (code-char ?n) ?x))))
922

```

923 2.6.2 Strings

924 A string is a list of characters. One way of referring to strings is through the use of the string syntax described in *Section 2.1.3, Lexemes*. In this method, we refer to the string `abc` by enclosing it in double quotes, such as, `"abc"`.

926 A second way is through the use of character blocks, the block syntax described in *Section 2.1.3, Lexemes*. In this method, we refer to the string `abc` by prefixing with the character `#`, a positive integer indicating the length, the letter `q`, and the characters of the string, for example, `#3qabc`.

930 A third way of referring to strings is to use the `listof` function. For example, we can denote the string `abc` by a term of the form `(listof #\a #\b #\c)`. The advantage of the `listof` representation over the preceding representations is that it allows us to quantify over characters within strings. For example, the following sentence says that all 3 character strings beginning with `a` and ending with `a` are `nice`.

```

935
936      (=> (character ?y) (nice (listof #\a ?y #\a)))
937

```

938 From this sentence, we can infer that various strings are `nice`.

```

939      (nice (listof #\a #\a #\a))
940      (nice "aba")
941      (nice #\Qaca)
942
943

```

944 2.7 Meta Knowledge

945 2.7.1 Naming Expressions

946 In formalizing knowledge about knowledge, we use a conceptualization in which expressions are treated as objects in the universe of discourse and in which there are functions and relations appropriate to these objects. In our conceptualization, we treat atoms as primitive objects with no subparts. We conceptualize complex expressions as lists of subexpressions (either atoms or other complex expressions). In particular, every complex expression is viewed as a list of its immediate subexpressions.

951 For example, we conceptualize the sentence `(not (p (+ a b c) d))` as a list consisting of the operator `not` and the sentence `(p (+ a b c) d)`. This sentence is treated as a list consisting of the relation constant `p` and the terms `(+ a b c)` and `d`. The first of these terms is a list consisting of the function constant `+` and the object constants `a`, `b` and `c`.

955 For Lisp programmers, this conceptualization is relatively obvious, but it departs from the usual conceptualization of formal languages taken in the mathematical theory of logic. It has the disadvantage that we cannot describe certain details of syntax such as parenthesization and spacing (unless we augment the conceptualization to include string representations of expressions as well). However, it is far more convenient for expressing properties of knowledge and inference than string-based conceptualizations.

961 In order to assert properties of expressions in the language, we need a way of referring to those expressions. There are two ways of doing this in FIPA KIF.

964

965 One way is to use the quote operator in front of an expression. To refer to the symbol john, we use the term 'john or,
 966 equivalently, (quote john). To refer to the expression (p a b), we use the term '(p a b) or, equivalently, (quote
 967 (p a b)).

968

969 With a way of referring to expressions, we can assert their properties. For example, the following sentence ascribes to
 970 the individual named john the belief that the moon is made of a particular kind of blue cheese.

971

```
972 (believes john '(material moon stilton))
```

973

974 Note that, by nesting quotes within quotes, we can talk about quoted expressions. In fact, we can write towers of
 975 sentences of arbitrary heights, in which the sentences at each level talk about the sentences at the lower levels.

976

977 Since expressions are first-order objects, we can quantify over them, thereby asserting properties of whole classes of
 978 sentences. For example, we could say that Mary believes everything that John believes. This fact together with the
 979 preceding fact allows us to conclude that Mary also believes the moon to be made of blue cheese.

980

```
981 (=> (believes john ?p) (believes mary ?p))
```

982

983 The second way of referring to expressions is FIPA KIF is to use the listof function. For example, we can denote a
 984 complex expression like (p a b) by a term of the form (listof 'p 'a 'b), as well as '(p a b).

985

986 The advantage of the listof representation over the quote representation is that it allows us to quantify over parts of
 987 expressions. For example, let us say that Lisa is more sceptical than Mary. She agrees with John, but only on the
 988 composition of things. The first sentence below asserts this fact without specifically mentioning moon or stilton. Thus, if
 989 we were to later discover that John thought the sun to be made of chilli peppers, then Lisa would be constrained to
 990 believe this as well.

991

```
992 (=> (believes john (listof 'material ?x ?y))  

  993 (believes lisa (listof 'material ?x ?y)))
```

994

995 While the use of listof allows us to describe the structure of expressions in arbitrary detail, it is somewhat awkward.
 996 For example, the term (listof 'material ?x ?y) is somewhat awkward. Fortunately, we can eliminate this difficulty
 997 using the up arrow (^) and comma (,) characters. Rather than using the listof function constant as described above,
 998 we write the expression preceded by ^ and , in front of any subexpression that is not to be taken literally. For example,
 999 we would rewrite the preceding sentence as follows.

1000

```
1001 (=> (believes john ^(material ,?x ,?y))  

  1002 (believes lisa ^(material ,?x ,?y)))
```

1003

1004 2.7.2 Types of Expressions

1005 In order to facilitate the encoding of knowledge about FIPA KIF, the language includes type relations for the various
 1006 syntactic categories defined in *Section 2.1, Syntax*.

1007

1008 For every individual variable *v*, there is an axiom asserting that it is indeed an individual variable. Each such axiom is a
 1009 defining axiom for the *indvar* relation.

1010

```
1011 (indvar (quote v))
```

1012

1013 For every sequence variable *s*, there is an axiom asserting that it is a sequence variable. Each such axiom is a defining
 1014 axiom for the *seqvar* relation.

1015

```
1016 (indvar (quote s))
```

1017

1018 For every word *w*, there is an axiom asserting that it is a word. Each such axiom is a defining axiom for the *word*
 1019 relation.

1020

```
(word (quote w))
```

Using this basic vocabulary and our vocabulary for lists, it is possible to define type relations for all types of syntactic expressions in FIPA KIF.

2.7.3 Changing Levels of Denotation

Logicians frequently use axiom schemata to encode (potentially infinite) sets of sentences with particular syntactic properties. As an example, consider the axiom schema shown below, where we are told that r stands for an arbitrary relation constant.

```
(=> (and (r 0) (forall (?n) (=> (r ?n) (r (1+ ?n)))) (forall (?n) (r ?n)))
```

This schema encodes infinitely many sentences, the principle of mathematical induction for named relations. The following sentences are instances:

```
(=> (and (p 0) (forall (?n) (=> (p ?n) (p (1+ ?n)))) (forall (?n) (p ?n)))
```

```
(=> (and (q 0) (forall (?n) (=> (q ?n) (q (1+ ?n)))) (forall (?n) (q ?n)))
```

Axiom schemata are differentiated from axioms due to the presence of meta-variables or other meta-linguistic notation (such as dots or star notation), together with conditions on the variables. They describe sentences in a language, but they are not themselves sentences in the language. As a result, they cannot be manipulated by procedures designed to process the language (presentation, storage, communication, deduction and so forth) but instead must be hard coded into those procedures.

As we have seen, it is possible in FIPA KIF to write expressions that describe FIPA KIF sentences. As it turns out, there is also a way to write sentences that assert the truth of the sentences so described. The effect of adding such meta-level sentences to a knowledge base is the same as directly including the (potentially infinite) set of described sentences in the knowledge base.

The use of such a language simplifies the construction of knowledge-based systems, since it obviates the need for building axiom schemata into deductive procedures. It also makes it possible for systems to exchange axiom schemata with each other and thereby promotes knowledge sharing.

The FIPA KIF truth predicate is called w_{tr} (which stands for “weakly true”). For example, we can say that a sentence of the form $(=> (p ?x) (q ?x))$ is true by writing the following sentence.

```
(wtr '(=> (p ?x) (q ?x)))
```

This may seem of limited utility, since we can just write the sentence denoted by the argument as a sentence in its own right. The advantage of the meta-notation becomes clear when we need to quantify over sentences, as in the encoding of axiom schemata. For example, we can say that every sentence of the form $(=> p p)$ is true with the following sentence. (The relation sentence can easily be defined in terms of `quote`, `listof`, `indvar`, `seqvar` and `word`.)

```
(=> (sentence ?p) (wtr ^ (=> ,?p ,?p)))
```

Semantically, we would like to say that a sentence of the form $(w_{tr} 'p)$ is true if and only if the sentence p is true. Unfortunately, this causes serious problems. Equating a truth function with the meaning it ascribes to w_{tr} quickly leads to paradoxes. The English sentence “This sentence is false” illustrates the paradox. We can write this sentence in FIPA KIF as shown below. The sentence, in effect, asserts its own negation.

```
(wtr (subst (name ^ (subst (name x) ^x ^ (truth ,x)))
            ^x
            ^ (not (wtr (subst (name x) ^x ^ (not (wtr ,x)))))))
```

l076 No matter how we interpret this sentence, we get a contradiction. If we assume the sentence is true, then we have a
 l077 problem because the sentence asserts its own falsity. If we assume the sentence is false, we also have a problem
 l078 because the sentence then is necessarily true.

l079
 l080 Fortunately, we can circumvent such paradoxes by slightly modifying the proposed definition of `wtr`. In particular, we
 l081 have the following axiom schema for all `p` that do not contain any occurrences of `wtr`. For all `p` that do contain
 l082 occurrences, `wtr` is false.

l083
 l084 $(\Leftrightarrow (\text{wtr } 'p) p)$

l085
 l086 With this modified definition, the paradox described above disappears, yet we retain the ability to write virtually all useful
 l087 axiom schemata as meta-level axioms.

l088
 l089 From the point of view of formalizing truth, `wtr` is a not particularly useful, since it fails to cover those interesting cases
 l090 where sentences contain the `truth` predicate. However, from the point of view of capturing axiom schemata not
 l091 involving the `truth` predicate, it works just fine. Furthermore, unlike the solutions to the problem of formalizing truth,
 l092 the framework presented here is easy for users to understand, and it is easy to implement.

l093
 l094 Two other constants round out FIPA KIF's level-crossing vocabulary. The term `(denotation t)` denotes the object
 l095 denoted by the object denoted by `t`. A quotation denotes the quoted expression; the denotation of any other object is
 l096 `bottom`. As with `wtr`, the denotation of a quoted expression is the embedded expression, provided that the expression
 l097 does not contain any occurrences of denotation. Otherwise, the value is undefined.

l098
 l099 $(= (\text{denotation } 't) t)$

l100
 l101 The term `(name t)` denotes the standard name for the object denoted by the term `t`. The standard name for an
 l102 expression `t` is `(quote t)`; the standard name for a non-expression is at the discretion of the user. (Note that there are
 l103 only a countable number of terms in FIPA KIF, but there can be worlds with uncountable cardinality; consequently, it is
 l104 not always possible for every object to have a unique name.)

l105

3 References

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4 Informative Annex A — Examples

1. The following FIPA ACL message with the content in FIPA KIF informs that `database-agent1` specializes handling the sentence `'(price ,?x ,?y)` where `?x` is a constant and `?y` is a number. Note that the communicative act `inform` takes a proposition as its content.

```

l122 (inform
l123   :sender
l124     (agent-identifier
l125       :name database-agent1)
l126   :receiver
l127     (agent-identifier
l128       :name facilitator1)
l129   :language FIPA-KIF
l130   :ontology ec-ontology
l131   :content
l132     (<= (specialist agent1 '(price ,?x ,?y))
l133         (constant ?x)
l134         (number ?y)))

```

2. This message informs that `database-agent1` conforms to the conformance profile `database-system` (see [ANSkif] for conformance details).

```

l138 (inform
l139   :sender
l140     (agent-identifier
l141       :name database-agent1)
l142   :receiver
l143     (agent-identifier
l144       :name facilitator1)
l145   :language FIPA-KIF
l146   :ontology ec-ontology
l147   :content
l148     (conformance-profile database-agent1 database-system))

```

3. This message informs that `database-agent1`'s conformance dimensions are `horn`, `non-recursive`, `simple`, `first-order`, `universal` and `baselevel` (see [ANSkif] for conformance details).

```

l153 (inform
l154   :sender
l155     (agent-identifier
l156       :name database-agent1)
l157   :receiver
l158     (agent-identifier
l159       :name facilitator1)
l160   :language FIPA-KIF
l161   :ontology ec-ontology
l162   :content
l163     (conformance-dimension database-agent1
l164       (horn non-recursive simple first-order universal baselevel)))

```

4. This message denies the message of the example in 1. Note that the communicative act `disconfirm` takes a proposition as its content.

```

l169 (disconfirm
l170   :sender
l171     (agent-identifier
l172       :name database-agent1)
l173   :receiver
l174     (agent-identifier
l175       :name facilitator1)

```

```

|177      :language FIPA-KIF
|178      :ontology ec-ontology
|179      :content
|180        (<= (specialist agent1 '(price ,?x ,?y))
|181          (constant ?x) (number ?y)))
|182

```

5. This message expresses a query by the agent, `facilitator1` to the agent, `database-agent1`. Note that the communicative act `query-ref` takes an object as its content.

```

|185      (query-ref
|186        :sender
|187          (agent-identifier
|188            :name facilitator1)
|189        :receiver
|190          (agent-identifier
|191            :name database-agent1)
|192        :language FIPA-KIF
|193        :ontology ec-ontology
|194        :content
|195          (kappa (?make ?door ?price)
|196            (and (car ?car) (make ?car ?make)
|197              (doors ?car ?doors) (price ?car ?price))))
|198
|199

```

6. This message expresses the answer to the query of the previous example by the agent, `database-agent1` to the agent, `facilitator1`:

```

|202      (inform
|203        :sender
|204          (agent-identifier
|205            :name database-agent1)
|206        :receiver
|207          (agent-identifier
|208            :name facilitator1)
|209        :language FIPA-KIF
|210        :ontology ec-ontology
|211        :content
|212          (= (kappa (?make ?door ?price)
|213            (and (car ?car) (make ?car ?make)
|214              (doors ?car ?doors) (price ?car ?price)))
|215            '((Mercedes 4 100,000) (Honda 2 20,000) (Toyota 4 25,000))))
|216
|217

```

I218 **5 Informative Annex B — ChangeLog**

I219 **5.1 2003/01/28 - version C by FIPA Architecture Board**

I220 Entire document: Added omitted `>` characters, fixed some other omissions
I221